

Chapter 16 (Bueche & Jerde) *Electric Force and Fields*

**P04**  $F_g = GM_p^2/r^2$  &  $F_e = ke^2/r^2$ .  $F_g = F_e \Rightarrow M_p = e(k/G)^{1/2} = 1.86 \times 10^{-9} \text{ kg}$ .

**P11**  $m = 60 \text{ g}$ ;  $kq^2/r^2 = Gm^2/r^2$  gives  $q = m(k/G)^{1/2} = 5.17 \times 10^{-12} \text{ C}$ .

**P15** Let  $x$  be the position of the 4 nC charge. It can not be located between the two charges,  $-5 \text{ nC}$  and  $6 \text{ nC}$ , because both exert forces in the same direction.

$$F_4 = k(4.00)(-5.00)/x^2 + k(4.00)(6.00)/(x-1)^2 = 0$$

leads to  $-5.00/x^2 + 6.00/(x-1)^2 = 0$  or  $x^2 + 10.0x - 5.00 = 0$ . Solving this we obtain  $x = -5.00 - 30.0^{1/2} = -10.5 \text{ (m)}$ .

**P19** Because the charges are identical and located at the corners of an equilateral triangle, by symmetry, all of them experience the force of same magnitude equal to  $F = 2k(5.00 \times 10^{-6})^2 \cos 30.0^\circ / (0.100)^2 = 39.0 \text{ (N)}$  along the bisector of the angle, directed outward.

**P20**  $q_1 = q_2 = q_3 = q_4 = q = 4.0 \mu\text{C}$ ,  $a = 40 \text{ cm}$ , and  $b = 60 \text{ cm}$ .  $F_{2x} = F_{21} + F_{41}(b/r)$ ,  $F_{2y} = F_{31} + F_{41}(a/r)$ , where  $r^2 = a^2 + b^2$ ,  $F_{21} = kq^2/a^2$ ,  $F_{31} = kq^2/b^2$ , and  $F_{41} = kq^2/r^2$ .  $F_{2x} = 0.630 \text{ N}$  and  $F_{2y} = 1.05 \text{ N}$ .

**P24**  $L = 40 \text{ cm}$ ,  $\theta = 30^\circ = 2\alpha$  &  $m = 1.0 \text{ g}$ .  $F_e = T \sin \alpha$  &  $mg = T \cos \alpha$ .  $F_e = mg \tan \alpha = kq^2/(2L \sin \alpha)^2$ ,  $q = 2L(mg \sin^3 \alpha / \cos \alpha)^{1/2} = 1.12 \times 10^{-7} \text{ C}$ .

**P38**  $F_e = F_g$  or  $qE = mg \Rightarrow E = mg/q$ .

**P41**  $T \cos \theta = mg$  &  $T \sin \theta = qE \Rightarrow E = mg \tan \theta / q$ .

**P47** (a)  $F_e = k(9.00 \times 10^{-6})(5.00 \times 10^{-6}) / (0.500)^2 = 1.62 \text{ (N)}$ ; (b) After being touched,  $q_1 = q_2 = 2.00 \mu\text{C}$ ,  $F_e = 0.144 \text{ N}$ .

**P48** (a)  $F_e = ke^2/r^2 = k(1.60 \times 10^{-19})^2 / (0.530 \times 10^{-10})^2 = 8.20 \times 10^{-8} \text{ (N)}$ ; (b)  $m_e v^2 / r = F_e$ , so  $v = (F_e r / m_e)^{1/2} = 2.18 \times 10^6 \text{ m/s}$ .

**P51** The net electric field at the center is zero due to the symmetry of charge distribution.

**P55** (a)  $a_y = -eE/m_e$ ,  $y = at^2/2 = -eEt^2/2m_e$ ; (b)  $t = x/v_{x0}$ ,  $y = (eE/2mev_{x0}^2)x^2$ .

**P58** (a) By symmetry,  $E_y = 0$  &  $E_x = 2(kq/r^2) \cos \theta$ , where  $\cos \theta = b/(b^2 + y^2)^{1/2}$ .  $E_x = 2kqb/(b^2 + y^2)^{1/2}$ ; (b) As  $y \gg b$ ,  $E_x = 2kqb/y^3$ .

**P60**  $E_y = 0$  &  $E_x = kq/(x+b)^2 - kq/(x-b)^2$ . Using  $1/(x+b)^2 = (1-2b/x)/x^2$  &  $1/(x-b)^2 = (1+2b/x)/x^2$  for  $b/x \ll 1$ , we obtain  $E_x = 4kqb/x^3$ .

## 第16章 (Bueche & Jerde) 電力與電場

**庫倫定律(Coulomb's Law)：** 法人庫倫(1736–1806)於 1785 年提出

兩點電荷間的作用力與兩點電荷乘積成正比，與兩點電荷間距離平方成反比，作用力方向為沿兩點電荷之連線方向， $\vec{F}_{21} = k_e q_1 q_2 \hat{r}_{12} / r_{12}^2$ 。

**殼層定理：**(A).對一電荷均勻分佈之球殼而言，其與殼內電荷之靜電力作用為零。(B).對一電荷均勻分佈之球(球殼)而言，其與球(球殼)外電荷之靜電力作用儼然整個球(球殼)之電荷均集中於球(殼)心。(C).對一電荷均勻分佈之球而言，其與球內點電荷之電力作用與到球心距離成正比。

**電場(力)線性質：**

1.靜電場線從正電荷出發，而結束於負電荷；2.從電荷發出或結束於電荷之場線數正比於電荷大小；3.場線的切線方向表示空間該點電場之方向；4.電場強度正比於場線密度(通過單位截面積之場線數目)；5.場線決不相交。 *注意：* 場線並非帶電質點之運動路徑。

**高斯定律：** 通過任一封閉曲面的電通量等於該封閉曲面所包圍的淨電荷除以 $\epsilon_0$ ，

$$\oint \vec{E} \cdot d\vec{A} = q_{net} / \epsilon_0。$$

在電場中之導體：**(A)**在靜電情況下，導體內部的電場為零。**(B)**在靜電情況下，導體內部沒有多餘(淨)電荷；如有多餘電荷必留駐於導體表面。**(C)**在靜電情況下，導體表面處的電場垂直於導體表面，而電場大小為 $\sigma / \epsilon_0$ ， $\sigma$ 為表面電荷密度。