

Chapter 07 (Bueche & Jerde) *Motion in a Circle*

Note that 1 rev =  $2\pi$  rad =  $360^\circ$ .

**P05**  $\omega = 2\pi/60 = 0.105$  (rad/s) .

**P11** (a)  $\alpha = (\omega_f - \omega_i)/t = [(3.75/60 - 0)]/22.0 = 2.84 \times 10^{-3}$  (rev/s<sup>2</sup>); (b)  $\theta = (\frac{1}{2})(\omega_i + \omega_f)t = 0.5(0 + 3.75/60)(22) = 0.688$  (rev) .

**P13**  $\theta = (\frac{1}{2})(\omega_i + \omega_f)t$ ,  $9.5 = 0.5(\omega_i)(18.5)$ ,  $\omega_i = 1.03$  rev/s .

**P21** (a)  $\omega = 2\pi/86400$ ;  $v = r\omega = (6.37 \times 10^6)\omega = 463$  (m/s); (b)  $r = 0$ ,  $v = 0$  .

**P22** (a)  $v = r\omega = (1.50 \times 10^{11}) [2\pi/(365.25 \times 86400)] = 2.99 \times 10^4$  (m/s) .

**P27** (a)  $x = \underline{v}t = (6.6)(38)/2 = 125$  (m); (b)  $\theta = x/r = 125/(0.625/2) = 401$  (rad) =  $63.9$  (rev) .

**P29**  $\omega_0 = 1660$  rev/min =  $174$  rad/s,  $\omega_f = 0$  &  $t = 16$  s: (a)  $\alpha = (\omega_f - \omega_0)/t = 109$  (rad/s<sup>2</sup>),  $\theta = (\omega_0/2)t = 221$  (rev); (b)  $x = r\theta = (0.0625)(221)(2\pi) = 87.0$  (m) .

**P31**  $\omega = v/r$ ,  $\omega_f - \omega_i = \alpha t$ ,  $\alpha = v_f/(rt) = 17.5/(0.40 \times 23.6) = 1.85$  (rad/s<sup>2</sup>);  $\theta = (\frac{1}{2})\alpha t^2 = 0.5(1.85)(23.6^2) = 515$  (rad) =  $82.0$  (rev) .

**P36**  $f = mv^2/r \leq \mu mg$ ,  $\mu \geq v^2/(gr) = r\omega^2/g = (0.30)[(33.3)(2\pi/60)]^2/9.80$ ,  $\mu \geq 0.372$  .

**P37**  $a_c = r\omega^2 = 5.3g$ ,  $(5.3)(9.80) = (11.3)(\omega^2)$ ,  $\omega^2 = 4.596$ ,  $\omega = 2.144$  rad/s =  $0.340$  rev/s .

**P38** Let  $F$  be the force of the pail acting on the water.  $F + mg = mv^2/r$ ,  $v^2 \geq gr$ ,  $v_{min} = \sqrt{gr} = \sqrt{(9.8)(0.72)} = 2.66$  (m/s) .

**P41**  $F_c = mr\omega^2$ ,  $(12,000)(9.80) = (0.085)\omega^2$ ,  $\omega = 1176$  rad/s =  $187$  rev/s .

**P42**  $F_N = mg$  &  $F_c = F_s \leq \mu_s F_N \Rightarrow mv^2/r \leq \mu_s(mg)$ ,  $v \leq \sqrt{\mu_s gr} = \sqrt{0.85 \times 9.8 \times 31.5} = 16.2$  (m/s) .

**P47**  $M_m = 4\pi\rho R_m^3/3$ ,  $M_e = 4\pi\rho R_e^3/3$ ,  $g_m = GM_m/R_m^2$  &  $g_e = GM_e/R_e^2$ :  $g_e/g_m = (M_e/M_m)(R_m^2/R_e^2) = R_e/R_m$ ,  $R_m = R_e(g_m/g_e) = R_e/6$  .

**P48**  $T = 87$  min &  $r = 6500$  km.  $GmM/r^2 = mv^2/r$  &  $T = 2\pi r/v \Rightarrow M = 4\pi^2 r^3/(GT^2) = 5.96 \times 10^{24}$  (kg) .

**P51** Let the tension in the string be  $T$ .  $F_x$ :  $T \sin\theta = mr\omega^2$  &  $F_y$ :  $T \cos\theta = mg$ ;  $\tan\theta = r\omega^2/g = (6.8)[0.045(2\pi)]^2/9.80 = 0.0555$ , giving  $\theta = 3.18^\circ$  .

**P52**  $mg \cos\theta - F_N = mv^2/R$ . Constant of E gives  $v^2 = 2gh = 2gR(1 - \cos\theta)$ .  $3mg \cos\theta - F_N = 2mg$ ,  $3mg \cos\theta \geq 2mg$ ,  $\cos\theta \geq 2/3 \Rightarrow \cos\theta_c = 2/3$  .

**P54**  $F_N \sin\theta = mg$  &  $F_N \cos\theta = mv^2/r$ .  $\tan\theta = gr/v^2$ , or  $v = \sqrt{gr/\tan\theta}$  .

**P56** Let  $m/M = r$ .  $MgR(1 + \cos 60^\circ) = mv_b^2/2$ ,  $v_b^2 = 3gR$  ... ①;  $v_{2f} = 2Mv_b/(m+M) = 2v_b/(1+r)$  ... ②;  $v_{top}^2 = v_{2f}^2 - 2g(2R)$  ... ③.  $v_{top}^2 = 12gR/(1+r)^2 - 4gR \geq gR$ ,  $(1+r)^2 \leq 12/5$ ,  $r \leq 0.549$  .

**P59** Let  $T_i$  and  $T_o$  be the tensions in the inner and outer strings, respectively. (a)  $T_o = m\omega^2(2L)$  and  $T_i - T_o = m\omega^2 L$ , giving  $T_i = 3m\omega^2 L$ .  $T_i > T_o$ . The inner string will break first. (b)  $\omega^2 = T_i/(3mL) = 235/[3(0.500)(0.6)] = 261.1$ ,  $\omega = 16.2$  rad/s =  $2.57$  rev/s .