

Chapter 04 (Bueche & Jerde) *Static Equilibrium*

**P03**  $\vec{F}_1$ : 240 N,  $30^\circ$  relative to  $x$  axis;  $\vec{F}_2$ : 320 N,  $120^\circ$  relative to  $x$  axis;  $\vec{F}_3$ :  $F_3$ ,  $\theta_3$  relative to  $-y$  axis. By  $F_1/\sin(120^\circ+\theta_3) = F_2/\sin(150^\circ-\theta_3) = F_3/\sin(90^\circ)$ ,  $4\sin\theta' = 3\sin\theta'$ , where  $\theta' = \theta + 30^\circ$  or  $\theta' = 36.9^\circ$ . So  $F = 400$  N &  $\theta = 6.9^\circ$ .

**P05**  $m_1g = m_2g = 90$  N.  $T_1 = T_2 = 90$ N. (a)  $M = 0$ ,  $T_3 = T_2 + T_1 = 180$  N; (b)  $Mg = 25$  N,  $T_3 = T_1 + T_2 + Mg = 205$  N.

**P07**  $F_h = 390$  N &  $\theta = 70^\circ$ .  $F \cos \theta = F_h$  &  $F \sin \theta = W \Rightarrow W = F_h \tan \theta = 1072$  N.

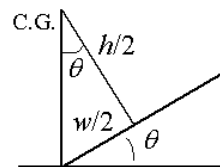
**P08**  $F = W \tan \theta$ ,  $W = F/\tan \theta = 240/\tan 30^\circ = 416$  (N).

**P09 & P10**  $F = W \tan \theta$ ,  $\tan \theta = F/W = 310/575$ ,  $\theta = 28.3^\circ$ .  $T = \sqrt{F^2 + W^2} = \sqrt{310^2 + 575^2} = 653$  (N).

**P19**  $W_1 = 600$  N.  $T_1 = T_2 = T_4 = W_2$ .  $T_1 = T_2 = W_1/2 = 300$  N and  $T_3 = T_2 + T_4 = 600$  N.

**P20**  $\Sigma F_y = 3T - mg = 0 \Rightarrow T = mg/3 = 540/3 = 180$  (N).

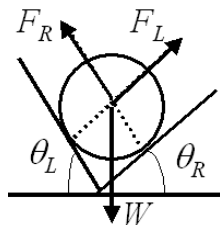
**P41** The critical angle  $\theta_c$  occurs when the center of gravity is directly above the lower contact. Thus we have  $\tan \theta_c = w/h$ , where  $w$  and  $h$  are the width and height, respectively. So,  $\theta_c = \tan^{-1}(1/2.5) = 21.8^\circ$ .



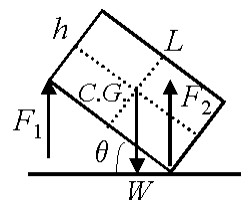
**Q.** 物體於粗糙斜面上下滑臨界角度  $\theta_{c,slip}$  為何?

**P34**  $L = 2$  m,  $F_L = 260$  N &  $F_R = 200$  N. Taking the center of gravity as the pivot point  $F_L x = F_R(L-x)$ ,  $x = LF_R/(F_L+F_R) = 0.870$  m.

**P42**  $W = 80$  N,  $\theta_L = 60^\circ$  &  $\theta_R = 40^\circ$ .  $F_{net,y} = 0$ :  $F_L \cos \theta_L + F_R \cos \theta_R = W$  &  $F_{net,x} = 0$ :  $F_L \sin \theta_L = F_R \sin \theta_R \Rightarrow F_L = W \sin \theta_R / \sin(\theta_L + \theta_R) = 52.2$  N &  $F_R = W \sin \theta_L / \sin(\theta_L + \theta_R) = 70.4$  N.



**P50** Taking the torques about the center of gravity:  $F_1 \ell_1 = F_2 \ell_2$ , where  $\ell_1$  and  $\ell_2$  are the lever arms for  $F_1$  and  $F_2$ , respectively. Using  $h = 0.4L$  &  $\theta = 37^\circ$ , from the geometry of the figure,  $\ell_1 = (L/2) \cos \theta + (h/2) \sin \theta = 0.52L$  &  $\ell_2 = L \cos \theta - \ell_1 = 0.28L$ . Comparing  $\ell_1 > \ell_2$ , therefore,  $F_2 > F_1$ .



**P21\***  $\tau = \ell F = (r \sin \theta)F$  &  $\ell = 5.00$  m.  $\tau_{90} = \tau_{50} = 0$ ,  $\tau_{60} = [2.50 \sin(-90^\circ)](60.0) = -150$  (N·m),  $\tau_{80} = (2.50 \sin 37^\circ)(80.0) = 120$  (N·m),  $\tau_{70} = (5.00 \sin 120^\circ)(70.0) = 303$  (N·m).

**P48\***  $R = 52.5$  cm,  $h = 18.0$  cm &  $W = 1230$  N. Taking the torques about the contact point A,  $\tau_{cw} \geq \tau_{ccw} \Rightarrow$

$$F_{min}(2R-h) = W\sqrt{R^2 - (R-h)^2} \Rightarrow F_{min} = 559$$
 N.

**Q.** 有否更省力的方向，將圓盤推上平台?

