## Chapter 2 Straight Line Motion

77．Assuming the horizontal velocity of the ball is constant，the horizontal displacement is $\Delta x=v \Delta t$ ， where $\Delta x$ is the horizontal distance traveled，$\Delta t$ is the time，and $v$ is the（horizontal）velocity．With $v=$ $160 \mathrm{~km} / \mathrm{h}=44.4 \mathrm{~m} / \mathrm{s}$ ，we have

$$
\Delta t=\frac{\Delta x}{\Delta t}=\frac{18.4}{44.4}=0.414 \text { (s). }
$$

04．With $1 \mathrm{~m} / \mathrm{s}=3.6 \mathrm{~km} / \mathrm{h}$ ，Huber＇s speed is

$$
v_{0}=(200 \mathrm{~m}) /(6.509 \mathrm{~s})=30.72 \mathrm{~m} / \mathrm{s}=110.6 \mathrm{~km} / \mathrm{h} .
$$

Since Whittingham beat Huber by $19.0 \mathrm{~km} / \mathrm{h}$ ，his speed is $v_{1}=110.6+19.0=129.6(\mathrm{~km} / \mathrm{h})$ ，or $36.00 \mathrm{~m} / \mathrm{s}$ ．Thus， the time through a distance of 200 m for Whittingham is

$$
\Delta t=\Delta x / v_{1}=(200 \mathrm{~m}) /(36.00 \mathrm{~m} / \mathrm{s})=5.554 \mathrm{~s} .
$$

05．Using $x=3 t-4 t^{2}+t^{3}$ with SI units understood is efficient（and is the approach we will use），but if we wished to make the units explicit we would write $x=(3 \mathrm{~m} / \mathrm{s}) t-\left(4 \mathrm{~m} / \mathrm{s}^{2}\right) t^{2}+\left(1 \mathrm{~m} / \mathrm{s}^{3}\right) t^{3}$ ．We will quote our answers to one or two significant figures，and not try to follow the significant figure rules rigor－ ously．（a）Plugging in $t=1 \mathrm{~s}$ yields $x=3-4+1=0$ ． （b）With $t=2$ s we obtain $x=3(2)-4(2)^{2}+(2)^{3}=-2$ （m）．（c）With $t=3 \mathrm{~s}$ we have $x=0 \mathrm{~m}$ ．（d）Plug－ ging in $t=4 \mathrm{~s}$ gives $x=12 \mathrm{~m}$ ．For later reference，we also note that the position at $t=0$ is $x=0$ ．（e）The position at $t=0$ is subtracted from the position at $t$ $=4 \mathrm{~s}$ to find the displacement $x=12 \mathrm{~m}$ ．（f）The po－ sition at $t=2 \mathrm{~s}$ is subtracted from the position at $t=$ 4 s to give the displacement $x=14 \mathrm{~m}$ ．Eq．2－2，then， leads to $v_{\mathrm{av}}=\Delta x / \Delta t=14 / 2=7(\mathrm{~m} / \mathrm{s})$ ．（g）The fi－ gure is shown for horizon－ tal axis of $0 \leq t \leq 4 \mathrm{~s}$ ．Draw a straight line from the point at $(2,-2)$ to that at $(4,12)$ ，whose slope give the answer for part（f）．
 07．Converting to seconds，the running times are $t_{1}$ $=147.95 \mathrm{~s}$ and $t_{2}=148.15 \mathrm{~s}$ ，respectively．If the run－ ners were equally fast，then

$$
S_{a v 1}=S_{a v 2} \Rightarrow L_{1} / t_{1}=L_{2} / t_{2}
$$

From this we obtain $L_{2}-L_{1}=$

$$
\left(\frac{t_{2}}{t_{1}}-1\right) L_{1}=\left(\frac{148.15}{147.95}-1\right) L_{1}=0.00135 L_{1} \approx 1.4 \mathrm{~m}
$$

where we set $L_{1} \approx 1000 \mathrm{~m}$ in the last step．Thus，if $L_{1}$ and $L_{2}$ are no different than about 1.4 m ，then runner 1 is indeed faster than runner 2．However，if $L_{1}$ is shorter than $L_{2}$ by more than 1.4 m ，then runner 2 would actually be faster．
17．We use Eq．2－2 for average velocity and Eq．2－4 for instantaneous velocity，and work with distances in centimeters and times in seconds．（a）We plug into the given equation for $x$ for $t=2.00 \mathrm{~s}$ and $t=$
3.00 s and obtain $x_{2}=21.75 \mathrm{~cm}$ and $x_{3}=50.25 \mathrm{~cm}$ ， respectively．The average velocity during the time interval $2.00 \leq t \leq 3.00 \mathrm{~s}$ is

$$
v_{a v}=\frac{\Delta x}{\Delta t}=\frac{50.25-21.75}{3.00-2.00},
$$

which yields $v_{\mathrm{av}}=28.5 \mathrm{~cm} / \mathrm{s}$ ．（b）The instantaneous velocity is $v=d x / d t=4.5 t^{2}$ ，which，at time $t=2.00 \mathrm{~s}$ ， yields $v=4.5)(2.00)^{2}=18.0(\mathrm{~cm} / \mathrm{s})$ ．（c）At $t=3.00 \mathrm{~s}$ ， the instantaneous velocity is $v=(4.5)(3.00)^{2}=40.5$ （cm／s）．（d）At $t=2.50 \mathrm{~s}$ ，the instanttaneous velocity is $v=(4.5)(2.50)^{2}=28.1(\mathrm{~cm} / \mathrm{s})$ ．（e）Let $t_{m}$ stand for the moment when the particle is midway be－ tween $x_{2}$ and $x_{3}$［that is，when the particle is at $x_{m}=$ $\left.\left(x_{2}+x_{3}\right) / 2=36 \mathrm{~cm}\right]$ ．Therefore，

$$
x_{m}=9.75+1.5 t_{m}{ }^{3} \Rightarrow t_{m}=2.596 \mathrm{~s} .
$$

Thus，the instantaneous speed at this time is $v=4.5 \times$ $(2.596)^{2}=30.3(\mathrm{~cm} / \mathrm{s})$ ．（f）The answer to part（a）is given by the slope of the straight line between $t=2$ $\& t=3$ in this $x$－vs－$t$ plot． The answers to parts（b）， （c），（d）and（e）correspond to the slopes of tangent lines（not shown but easi－ ly imagined）to the curve at the appropriate points．


20．（a）Taking derivatives of $x(t)=12 t^{2}-2 t^{3}$ ，we obtain the velocity and the acceleration functions：

$$
v(t)=24 t-6 t^{2} \quad \text { and } \quad a(t)=24-12 t
$$

with length in meters and time in seconds．Plugging in the value $t=3$ yields $x(3)=54 \mathrm{~m}$ ．．（b）Similarly， plugging in the value $t=3$ yields $v(3)=18 \mathrm{~m} / \mathrm{s}$ ．（c） For $t=3, a(3)=-12 \mathrm{~m} / \mathrm{s}^{2}$ ．（d）At the maximum $x$ ， we must have $v=0$ ；eliminating the $t=0$ root，the velocity equation reveals $t=24 / 6=4$（s）for the time of maximum $x$ ．Plugging $t=4$ into the equation for $x$ leads to $x=64 \mathrm{~m}$ for the largest $x$ value reached by the particle．（e）From（d），we see that the $x$ reaches its maximum at $t=4.0 \mathrm{~s}$ ．（f）A maximum $v$ re－ quires $a=0$ ，which occurs when $t=24 / 12=2.0$（s）． This，inserted into the velocity equation，gives $v_{\text {max }}$ $=24 \mathrm{~m} / \mathrm{s}$ ．（g）From（f），we see that the maxi－mum of $v$ occurs at $t=24 / 12=2.0$（s）．（h）In part（e）， the particle was（momentarily）motionless at $t=4 \mathrm{~s}$ ． The acceleration at that time is readily found to be $24-12(4)=-24\left(\mathrm{~m} / \mathrm{s}^{2}\right)$ ．（i）The average velocity is defined by Eq．2－2，so we see that the values of $x$ at $t$ $=0$ and $t=3 \mathrm{~s}$ are needed；these are，respectively，$x$ $=0$ and $x=54 \mathrm{~m}$［found in part（a）］．Thus，

$$
v_{\mathrm{av}}=(54-0) /(3-0)=18(\mathrm{~m} / \mathrm{s})
$$

22．We use Eq．2－2（average velocity）and Eq．2－7（av－ erage acceleration）．Regarding our coordinate choices，
the initial position of the man is taken as the origin and his direction of motion during $5 \mathrm{~min} \leq t \leq 10$ min is taken to be the $+x$ direction．We also use the fact that $\Delta x=v \Delta t^{\prime}$ when the velocity is constant during a time interval $\Delta t^{\prime}$ ．（a）The entire interval considered is $\Delta t=8-2=6$（min）which is equivalent to 360 s，whereas the sub－interval in which he is mo－ $v i n g$ is only $\Delta t^{\prime}=8-5=3(\mathrm{~min})=180(\mathrm{~s})$ ．His posi－ tion at $t=2 \mathrm{~min}$ is $x=0$ and his position at $t=8 \mathrm{~min}$ is $\quad x=v \Delta t^{\prime}=(2.2)(180)=396(\mathrm{~m})$ ．Therefore，

$$
v_{\mathrm{av}}=(396 \mathrm{~m}-0) /(360 \mathrm{~s}-0)=1.10 \mathrm{~m} / \mathrm{s}
$$

（b）The man is at rest at $t=2 \mathrm{~min}$ and has velocity $v$ $=2.2 \mathrm{~m} / \mathrm{s}$ at $t=8 \mathrm{~min}$ ．Thus，keeping the answer to 3 significant figures，

$$
a_{\mathrm{av}}=(2.2 \mathrm{~m} / \mathrm{s}-0) /(360 \mathrm{~s}-0)=0.00611 \mathrm{~m} / \mathrm{s}^{2}
$$

（c）Now，the entire interval considered is $\Delta t=9-3$ $=6(\mathrm{~min})(360 \mathrm{~s}$ again），whereas the sub－interval in which he is moving is $\Delta t^{\prime}=9-5=4(\mathrm{~min})=240(\mathrm{~s})$ ． His position at $t=3 \mathrm{~min}$ is $x=0$ and his position at $t$ $=9 \mathrm{~min}$ is $x=v \Delta t^{\prime}=(2.2)(240)=528(\mathrm{~m})$ ．There fore，$\quad v_{\mathrm{av}}=(528 \mathrm{~m}-0) /(360 \mathrm{~s}-0)=1.47 \mathrm{~m} / \mathrm{s}$ ．
（d）The man is at rest at $t=3 \mathrm{~min}$ and has velocity $v$ $=2.2 \mathrm{~m} / \mathrm{s}$ at $t=9 \mathrm{~min}$ ．Consequently，$a_{\mathrm{av}}=2.2 / 360=$ $0.00611\left(\mathrm{~m} / \mathrm{s}^{2}\right)$ just as in part（b）．（e）The horizon－ tal line near the bottom of this $x$－vs－$t$ graph re－ presents the man stand－ ing at $x=0$ for $0 \leq t<$ 300 s and the linearly rising line for $300 \mathrm{~s} \leq t$ $\leq 600$ s represents his
 constant－velocity
motion．The dotted lines represent the answers to part（a）and（c）in the sense that their slopes yield those results．The graph of $v$－vs－$t$ is not shown here， but would consist of two horizontal＂steps＂（one at $v=0$ for $0 \leq t<300 \mathrm{~s}$ and the next at $v=2.2 \mathrm{~m} / \mathrm{s}$ for $300 \mathrm{~s} \leq t \leq 600 \mathrm{~s}$ ）．The indications of the average accelerations found in parts（b）and（d）would be dotted lines connecting the＂steps＂at the appropriate $t$ values（the slopes of the dotted lines re－ presenting the values of $a_{\mathrm{av}}$ ）．Using the above value for $\theta$ and $h=1.7 \mathrm{~m}$ ，we have $r=5.2 \times 10^{6} \mathrm{~m}$ ．
29．We separate the motion into two parts，and take the direction of motion to be positive．In part 1， the vehicle accelerates from rest to its high－est speed；we are given $v_{0}=0 ; v=20 \mathrm{~m} / \mathrm{s}$ and $a=2.0$ $\mathrm{m} / \mathrm{s}^{2}$ ．In part 2 ，the vehicle decelerates from its highest speed to a halt；we are given $v_{0}=20 \mathrm{~m} / \mathrm{s}$ ；$v$ $=0$ and $a=-1.0 \mathrm{~m} / \mathrm{s}^{2}$（negative because the acelera－ tion vector points opposite to the direction of motion）．
（a）From Table 2－1，we find $t_{1}$（the duration of part
1）from $v=v_{0}+a t$ ．In this way， $20=0+2.0 t_{1}$ yields
$t_{1}=10 \mathrm{~s}$ ．We obtain the duration $t_{2}$ of part 2 from the same equation．Thus， $0=20+(-1.0) t_{2}$ leads to $t_{2}=20 \mathrm{~s}$ ，and the total is $t=t_{1}+t_{2}=30 \mathrm{~s}$ ．
（b）For part 1 ，taking $x_{0}=0$ ，we use the equation $v^{2}$ $=v_{0}^{2}+2 a\left(x-x_{0}\right)$ from Table 2－1 and find

$$
x=\frac{v^{2}-v_{0}^{2}}{2 a}=\frac{20^{2}-0}{2(2.0)}=100(\mathrm{~m})
$$

This position is then the initial position for part 2， so that when the same equation is used in part 2 we
obtain

$$
x-100=\frac{v^{2}-v_{0}^{2}}{2 a}=\frac{0^{2}-20^{2}}{2(-1.0)}
$$

Thus，the final position is $x=300 \mathrm{~m}$ ．That this is also the total distance traveled should be evident （the vehicle did not＂backtrack＂or reverse its direc－ tion of motion）．
30．The acceleration found from Eq．2－11（or，sui－ tably interpreted，Eq．2－7）is

$$
\begin{gathered}
a=\Delta v / \Delta t=(1020 \mathrm{~km} / \mathrm{h}) /(1.4 \mathrm{~s}) \\
=(1020 \mathrm{~m}) /\left(3.6 \times 1.4 \mathrm{~s}^{2}\right)=202.4 \mathrm{~m} / \mathrm{s}^{2}
\end{gathered}
$$

In terms of the gravitational acceleration $g$ ，this is expressed as a multiple of $9.8 \mathrm{~m} / \mathrm{s}^{2}$ as follows：

$$
a=(202.4 / 9.8) g=20.6 g=21 g
$$

34．（a）Eq．2－15 is used for part 1 of the trip and Eq． 2－18 is used for part 2：$\quad \Delta x_{1}=v_{0,1} t_{1}+\frac{1}{2} a_{1} t_{1}{ }^{2}$ ，
where $a_{1}=2.25 \mathrm{~m} / \mathrm{s}^{2}$ and $\Delta x_{1}=900 / 4 \mathrm{~m}$ ，

$$
\Delta x_{2}=v_{2} t_{2}-\frac{1}{2} a_{2} t_{2}^{2}
$$

where $a_{2}=-0.75 \mathrm{~m} / \mathrm{s}^{2}$ and $\Delta x_{2}=3(900) / 4 \mathrm{~m}$ ．In ad－ dition，$v_{0,1}=v_{2}=0$ ．Solving these equations for the times and adding the results gives $t=t_{1}+t_{2}=56.6 \mathrm{~s}$ ．
（b）Eq．2－16 is used for part 1 of the trip：

$$
\begin{gathered}
v^{2}=\left(v_{0,1}\right)^{2}+2 a_{1} \Delta x_{1} \\
=0+2(2.25)(900 / 4)=1013\left(\mathrm{~m}^{2} / \mathrm{s}^{2}\right)
\end{gathered}
$$

which leads to $v=31.8 \mathrm{~m} / \mathrm{s}$ for the maximum speed．
99．We neglect air resistance，which justifies setting $a=-g=-9.8 \mathrm{~m} / \mathrm{s}^{2}$（taking down as the $-y$ direction）for the duration of the motion．We are allowed to use Table 2－1（with $\Delta y$ replacing $\Delta x$ ）because this is con－ stant acceleration motion．When something is thrown straight up and is caught at the level it was thrown from（with a trajectory similar to that shown in Fig．2－25），the time of flight $t$ is half of its time of ascent $t_{a}$ ，which is given by Eq．2－18 with $\Delta y=H$ and $v=0$（indicating the maximum point）．

$$
H=v t_{a}+\frac{1}{2} g t_{a}^{2} \Rightarrow t_{a}=\sqrt{2 H / g} .
$$

Writing these in terms of the total time in the air $t=$ $2 t_{a}$ we have $H=\frac{1}{8} g t^{2} \Rightarrow t=2 \sqrt{2 H / g}$ ．
We consider two throws，one to height $H_{1}$ for total time $t_{1}$ and another to height $H_{2}$ for total time $t_{2}$ ，and we set up a ratio：$\frac{H_{2}}{H_{1}}=\frac{g t_{2}^{2} / 8}{g t_{1}^{2} / 8}=\left(\frac{t_{2}}{t_{1}}\right)^{2}$
from which we conclude that if $t_{2}=2 t_{1}$（as is re－ quired by the problem）then $H_{2}=2^{2} H_{1}=4 H_{1}$ ．
$105^{\circ}$ ．We neglect air resistance，which justifies set－ ting $a=-g=-9.8 \mathrm{~m} / \mathrm{s}^{2}$（taking down as the $-y$ di－ rection）for the duration of the stone＇s motion．We are allowed to use Table 2－1（replacing $x$ by $y$ ）be－ cause the ball has constant acceleration motion（and we choose $y_{0}=0$ ）．（a）We apply Eq．2－16 to both measurements，with SI units understood．

$$
\begin{gathered}
v_{B}^{2}=v_{0}^{2}-2 g y_{B} \Rightarrow\left(\frac{1}{2} v\right)^{2}+2 g\left(y_{A}+3\right)=v_{0}^{2} \\
v_{A}^{2}=v_{0}^{2}-2 g y_{A} \Rightarrow v^{2}+2 g y_{A}=v_{0}^{2} .
\end{gathered}
$$

We equate the two expressions that each equal $v_{0}{ }^{2}$ and obtain

$$
\frac{1}{4} v^{2}+2 g y_{A}+6 g=v^{2}+2 g y_{A} \Rightarrow 6 g=\frac{3}{4} v^{2},
$$

which yields $v=(8 g)^{1 / 2}=8.85 \mathrm{~m} / \mathrm{s}$ ．（b）An object moving upward at $A$ with speed $v=8.85 \mathrm{~m} / \mathrm{s}$ will reach a maximum height $y-y_{A}=v^{2} / 2 g=4.00 \mathrm{~m}$ above point $A$（this is again a consequence of Eq．2－16， now with the＂final＂velocity set to zero to indicate the highest point）．Thus，the top of its motion is 1.00 m above point $B$ ．
111．${ }^{\text {• There }}$ is no air resistance，which makes it quite accurate to set $a=-g=-9.8 \mathrm{~m} / \mathrm{s}^{2}$（where downward is the $-y$ direction）for the duration of the fall．We are allowed to use Table 2－1（replacing $x$ by $y$ ）be－ cause this is constant acceleration motion；in fact， when the acceleration changes（during the process of catching the ball）we will again assume constant acceleration conditions；in this case，we have $a_{2}=$ $25 \mathrm{~g}=245 \mathrm{~m} / \mathrm{s}^{2}$ ．（a）The time of fall is given by Eq．2－15 with $v_{0}=0$ and $y=0$ ．Thus，

$$
t=\sqrt{2 y_{0} / g}=\sqrt{2(145) / 9.8}=5.44(\mathrm{~s}) .
$$

（b）The final velocity for its free－fall（which be－ comes the initial velocity during the catching pro－ cess）is found from Eq．2－16［other eqs．can be used but they would use the result from part（a）］．

$$
v=-\sqrt{v_{0}^{2}-2 g\left(y-y_{0}\right)}=-\sqrt{2 g y_{0}}=-53.3(\mathrm{~m} / \mathrm{s}) .
$$

where the negative root is chosen since this is a downward velocity．Thus，the speed is $|v|=53.3 \mathrm{~m} / \mathrm{s}$ ． （c）For the catching process，the answer to part（b） plays the role of an initial velocity（ $v_{0}=-53.3 \mathrm{~m} / \mathrm{s}$ ） and the final velocity must become zero．Using Eq． $2-16$ ，we find

$$
\Delta y_{2}=\frac{v^{2}-v_{0}^{2}}{2 a_{2}}=\frac{0-(-53.3)^{2}}{2(245)}=-5.80(\mathrm{~m})
$$

where the negative value of $\Delta y_{2}$ signifies that the distance traveled while arresting its motion is downward．
（如發現錯誤煩請告知，jyang＠mail．ntou．edu．tw，Thanks．）
Ex．2－1，Prob．2－71 \＆Ex．2－2，Prob．2－88．

112．We neglect air resistance，which justifies set－ ting $a=-g=-9.8 \mathrm{~m} / \mathrm{s}^{2}$（taking down as the $-y$ direc－ tion）for the duration of the motion．We are allowed to use Table 2－1（replacing $x$ by $y$ ）because this is constant acceleration motion．The ground level is taken to correspond to $y=0$ ．（a）With $y_{0}=h$ and $v_{0}$ replaced with $-v_{0}$ ，Eq．2－16 leads to

$$
v=\sqrt{\left(-v_{0}\right)^{2}-2 g\left(y-y_{0}\right)}=\sqrt{v_{0}^{2}+2 g h} .
$$

The positive root is taken because the problem asks for the speed（the magnitude of the velocity）．（b） We use the quadratic formula to solve Eq．2－15 for $t$ ， with $v_{0}$ replaced with $-v_{0}$ ，
$\Delta y=-v_{0} t-\frac{1}{2} g t^{2} \Rightarrow t=\frac{1}{g}\left(-v_{0}+\sqrt{\left(-v_{0}\right)^{2}-2 g \Delta y}\right)$.
where the positive root is chosen to yield $t>0$ ．
With $y=0$ and $y_{0}=h$ ，this becomes

$$
t=\frac{1}{g}\left(\sqrt{v_{0}^{2}+2 g h}-v_{0}\right) .
$$

（c）If it were thrown upward with that speed from height $h$ then（in the absence of air friction）it would return to height $h$ with that same downward speed and would therefore yield the same final speed（be－ fore hitting the ground）as in part（a）．（d）Having to travel up before it starts its descent certainly re－ quires more time than in part（b）．The calculation is quite similar，however，except for now having $+v_{0}$ in the equation where we had put in $-v_{0}$ in part（b）． The details follow：

$$
\Delta y=v_{0} t-\frac{1}{2} g t^{2} \Rightarrow t=\frac{1}{g}\left(v_{0}+\sqrt{v_{0}^{2}-2 g \Delta y}\right) .
$$

with the positive root again chosen to yield $t>0$ ． With $y=0$ and $y_{0}=h$ ，we obtain

$$
t=\frac{1}{g}\left(v_{0}+\sqrt{v_{0}^{2}+2 g h}\right) .
$$

挑戰題〉設直線賽車比賽總長為 $S$ ，若跑車前段加速 （ $a_{1}>0$ ），而後段減速 $\left(-a_{2}<\right.$ $0)$ ，試計算跑車所花時間。
Sol．Let the distance during
 the period $t_{1}$ of the acceleration $a_{1}$ be $S_{1}$ and the dis－ tance during the period $t_{2}$ of the acceleration $-a_{2}$ be $S_{2}$ ．The maximum speed of car is
$v_{\max }^{2}=2 a_{1} S_{1}=2 a_{2} S_{2}$ ．From $S=S_{1}+S_{2}$ ，we have $S_{1}=\frac{a_{2} S}{a_{1}+a_{2}}=\frac{1}{2} a_{1} t_{1}^{2} \quad$ and $S_{2}=\frac{a_{1} S}{a_{1}+a_{2}}=\frac{1}{2} a_{2} t_{2}^{2}$ ．
Solve them to find $t_{1}=\left[\frac{2 a_{2} S}{a_{1}\left(a_{1}+a_{2}\right)}\right]^{1 / 2}$ and
$t_{2}=\left[\frac{2 a_{1} S}{a_{2}\left(a_{1}+a_{2}\right)}\right]^{1 / 2}$ ，so $\Delta t=t_{1}+t_{2}=\left[\frac{2\left(a_{1}+a_{2}\right) S}{a_{1} a_{2}}\right]^{1 / 2}$.
Using $S=0.25 \mathrm{mi}=1320 \mathrm{ft}, a_{1}=24 \mathrm{ft} / \mathrm{s}^{2}$ ，and $a_{2}=$ $-32 \mathrm{ft} / \mathrm{s}^{2}$ leads to $\Delta t=13.9 \mathrm{~s}$ ．

## 重點整理—第2章 直線運動

宇宙萬物皆在動，但如何動？力學包含運動學與動力學；運動學是力學之初步。運動學旨在探討物體如何運動，即描述物體在空間的位置 $\boldsymbol{r}$ 與時間 $t$ 之關係， $\boldsymbol{r}=\boldsymbol{r}(t)$ ；只用＂空間＂及＂時間＂兩基本概念，無＂力＂與＂質量＂等概念。動力學：探討運動之起因，物體為什麼作這樣運動。即研討力，質點（或物體）以及運動物體之間的關係，或物體運動時所遵守的定律或法則一牛頓運動定律。一維或直線運動 $x=x(t)$ ，時間 $t_{1} \rightarrow 0 \Rightarrow t_{2} \rightarrow t$ ，
時距 $\Delta t \equiv t_{2}-t_{1} \rightarrow t$ ，


初位置 $x_{1} \equiv x\left(t_{1}\right) \rightarrow x_{0} \Rightarrow$ 末位置 $x_{2} \equiv x\left(t_{2}\right) \rightarrow x$,位移為＂位置之改變量＂$\Delta x \equiv x_{2}-x_{1} \rightarrow x-x_{0}$ ，只與初位置及末位置有關，但與運動細節無關。平均速度為＂單位時間之位移＂$v_{a v} \equiv \Delta x / \Delta t$ ， （瞬時）速度為位置之時變率 $v=d x / d t$ ，速率指（a）速度大小或（b）運動總路程除以時距初速度 $v_{1} \equiv v\left(t_{1}\right) \rightarrow v_{0} \Rightarrow$ 末速度 $v_{2} \equiv v\left(t_{2}\right) \rightarrow v$ ；速度改變量 $\Delta v \equiv v_{2}-v_{1} \rightarrow v-v_{0}$ ，平均加速度為單位時間之速度改變量 $a_{a v} \equiv \Delta v / \Delta t$ ， （瞬時）加速度為速度之時變率 $a=d v / d t=d^{2} x / d t^{2}$ ，一維等加速度運動 $a=a_{a v}=$ const．，
$v_{a v}=\frac{1}{2}\left(v_{0}+v\right)$ ，即‘初速度’與‘末速度’之平均值，
$\Delta v=a \Delta t=a t$ or $v=v_{0}+a t$ ，
$\Delta x=v_{a v} \Delta t=v_{0} t+\frac{1}{2} a t^{2}$, or $x=x_{0}+v_{0} t+\frac{1}{2} a t^{2}$, $v^{2}-v_{0}^{2}=2 a \Delta x$ ，or $v^{2}=v_{0}^{2}+2 a\left(x-x_{0}\right)$ ，
Note $v=0$ 表示運動停止或運動方向即將改變（即前後速度變號），該點為折返點；
自由下落運動：設鉛直方向之加速度為定值

$$
x \rightarrow y \text { and } a \rightarrow a_{y}=-g(\Delta y>0: \text { up })
$$

地表自由下落加速度 $g=9.8 \mathrm{~m} / \mathrm{s}^{2}=49 / 5 \mathrm{~m} / \mathrm{s}^{2}$ 。
－地震時地表加速度以 gal 表示， $1 \mathrm{gal}=1 \mathrm{~cm} / \mathrm{s}^{2}$ 。 －人類跑百米最快需 9.69 s （2009柏林，牙買加柏特） －據調查人與人之距離約 5～6人。•頸骨受傷／鞭様損傷：是車禍常見的症狀，主要因為車禍發生時，頭部及頸部的脊骨就如鞭子鞭動一樣，因突然而來的劇動而受傷。•基隆之 $g=9.78974 \mathrm{~m} / \mathrm{s}^{2}$ 。

## Why can a woodpecker survive the severe impacts with a tree limb？

為何豚木鳥激烈的撞擊大樹枝還能存活？
解題策略：1．問題瞭解嘛？2．單位正確嘛？3．答案合理嘛？4．讀懂圖形。 Note $d\left(x^{n}\right) / d x=n x^{n-1}$ 。
Q．某質點在某時刻的速度為 $+18 \mathrm{~m} / \mathrm{s}, 2.4 \mathrm{~s}$ 後速率變為 $30 \mathrm{~m} / \mathrm{s}$ 但往相反的方向．則在 2.4 s 内的平均加速度為（a）$+10 \mathrm{~m} / \mathrm{s}^{2}$ ；（b）$+20 \mathrm{~m} / \mathrm{s}^{2}$ ；（c）$-10 \mathrm{~m} / \mathrm{s}^{2}$ ； （d）$-20 \mathrm{~m} / \mathrm{s}^{2}$ 。 Q．車速為 $180 \mathrm{~km} / \mathrm{h}$ 之車子突然煞車，若煞車距離為 175 m ，試計算煞車過程之加速度。（Ans．$-7.14 \mathrm{~m} / \mathrm{s}^{2}$ ） $\boldsymbol{Q}$ 。設地表附近 $g=9.80 \mathrm{~m} / \mathrm{s}^{2}$ ，某球於離地 33.6 m 高處，以速率 $35.0 \mathrm{~m} / \mathrm{s}$ 鉛直上抛，試計算該球可抵達之最大高度（a）及於空中停留時間（b）．［Ans．（62．5＋33．6）m \＆ 8.00 s ］
motion，運動；kinematics，運動學；particle，質點；position位置；origin／zero point，原點；positive／negative direction，正／負的方向；axis（座標）軸；coordinate，座標；vector，向量；displacement，位移；distance，距離；total distance，總距離／路程；time interval，時距；travel，行進；slope，斜率； average velocity，平均速度；（instantaneous）velocity，（瞬時）速度；speed，速率；speedometer，速率錶；average acce－ leration，平均加速度；（instantaneous）acceleration（瞬時）加速度；constant acceleration，等加速度，free－fall，自由下落；derivative，道數／微商；tectonic plate，板塊；artery，動脈；whiplash injury，頸部扭傷；head restraint，頭枕； woodpecker，啄木鳥；beak，鳥啄；rat－tat，咚咚的聲音，敲擊聲；fanatical，狂熱的／入迷的；armadillo，犹狳（中南美產）；beat－up，用壞了的；pickup 臨時湊成的／偶然認識的； sprinter，短跑選手；energy conservation（EC）；Niagara Falls，尼加拉瓜瀑布；Porche，保時捷；NASCAR：Nation－ al Association of Stock Car Auto Racing，全國運動汽車競賽協會；jai alai，回力球（類似手球的室内遊戲，盛行於拉丁美洲）$\bullet 1$ knot $=1.852 \mathrm{~km} / \mathrm{h}$
－高速鐵路是指行車時速達二百公里以上的行車系統（電車），台灣高鐵（ 960105 管運通車）之新幹線電車平均行車速率 $230 \mathrm{~km} / \mathrm{h}(63.9 \mathrm{~m} / \mathrm{s})$ ，最高時速 300 $\mathrm{km} / \mathrm{h}$ ，台北至高雄左營距 345 km ，行車需 90 分。
－世上最快電車—法國 TGV 最高時速可達 574.8 km （357．2 英里），而上海磁浮車時速達 435 km 。 •1971 （美）阿波羅十五號太空人在月球表面，左手持鐵錘，右手拿羽毛，同時釋放，結果鐵錘與羽毛同時著地。 J1．＂交通與物理＂，黄定維及黄偉能，物理雙月刊， 24 卷 2 期（2004 年 4 月）334－337。J2．＂The evolution of transport＂，J．H．Ausubel and C．Marchetti，The In－ dustrial Physicist，April／May 2001，pp．20－24。

